

$$V = \{ A B C \}$$

$$\Gamma = \{ \boxed{A \rightarrow B}, \boxed{B \rightarrow C}, \boxed{C \rightarrow A} \}$$

A	B	C
a ₁	b ₁	c ₁
a ₂	b ₂	c ₂
a ₃	b ₂	c ₂

keys are: A, B, C

$R_1(AB)$, $R_2(BC)$
 $A \rightarrow B$, $B \rightarrow C$

$$V = \{A, B, C\}$$

$$F = \{A \rightarrow B, B \rightarrow C\}$$

$$P = \{A \rightarrow C, B \rightarrow C\}$$

$A \ B \ C$	$R_1 (A \ B)$
$a_1 \ b_1 \ c_1$	$a_1 \ b_1$
$a_2 \ b_2 \ c_1$	$a_2 \ b_2$
$R_1 \ \&R_2$	$R_2 (B \ C)$
$a_1 \ b_1 \ c_1$	$b_1 \ c_1$
$a_1 \ b_2 \ c_1$	$b_2 \ c_1$
$a_2 \ b_1 \ c_1$	
$a_2 \ b_2 \ c_1$	

$$\pi[AB] \mathcal{F}$$

$$= \{A \rightarrow B\}$$

$$\begin{array}{l} \downarrow \\ \{B \rightarrow A\} \end{array}$$

$$\mathcal{F} \models B \rightarrow A$$

$$\Rightarrow B \rightarrow A \in \mathcal{F}^+$$

$$\pi(B) \mathcal{F}$$

$$= \{B \rightarrow C, C \rightarrow B\}$$

$$\quad \quad \quad C \rightarrow A, A \rightarrow C$$

$$\left(\underline{A \rightarrow B}, \underline{B \rightarrow A}, \underline{B \rightarrow C}, \underline{C \rightarrow B} \right)$$

$$\checkmark \equiv \left(\underline{A \rightarrow B}, \underline{B \rightarrow C}, \underline{C \rightarrow A} \right)$$

$$\quad \quad \quad \begin{array}{l} B \rightarrow A \\ C \rightarrow B \end{array} \quad \mathcal{F} \quad A \rightarrow C$$

$$V = \{A B C\}$$

$$\mathcal{R} = \{A \rightarrow B, \underline{B \rightarrow C}\}$$

$$R_1: \{A B C\} \setminus \{C\} = \{A B\}$$

$$R_2: \{B C\}$$

$$V = \{A B C D\}$$

$$\mathcal{R} = \{A \rightarrow B, \underline{B \rightarrow C}, \underline{C \rightarrow D}\}$$

$$R_2: \{C D\}$$

$$R_1: \{A B C\} \rightarrow \begin{matrix} R_{12}: \{B C\} \\ R_{11}: \{A B\} \end{matrix}$$

$$V = \{ A B C \}$$

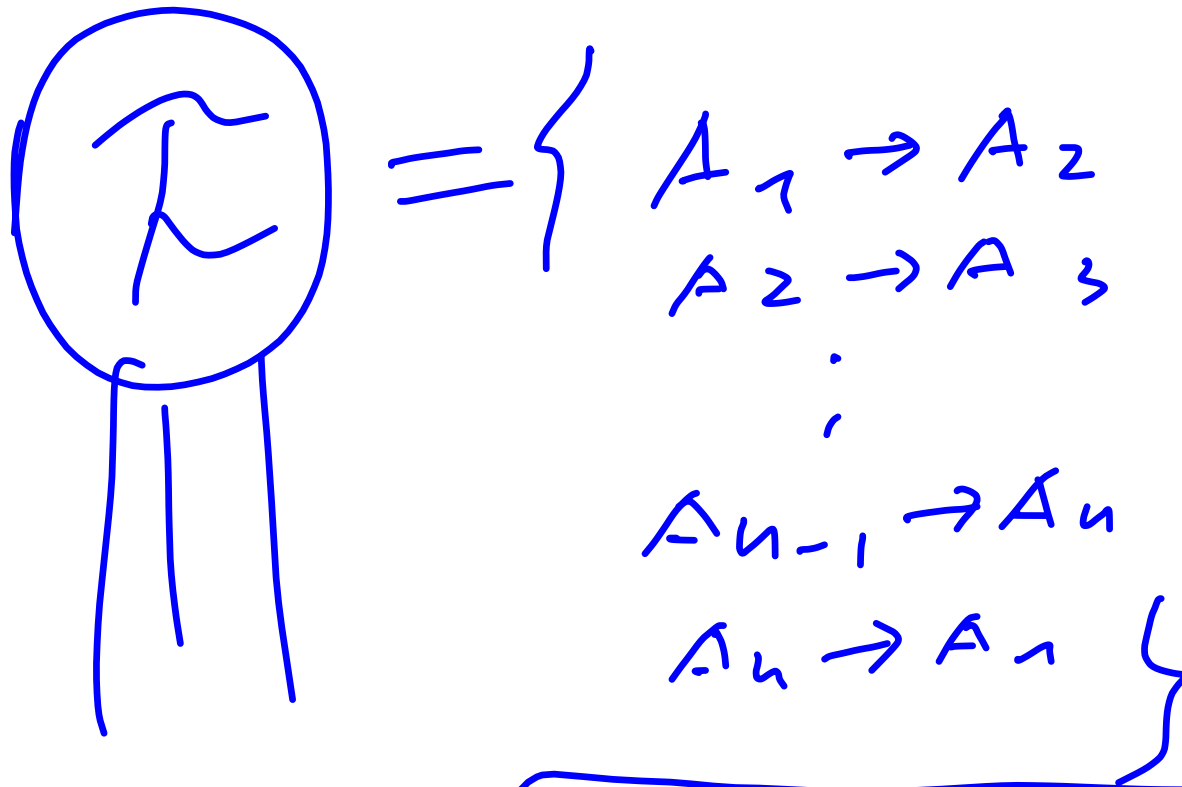
A	B	C
a_1, b_1, c_1		
a_1, b_2, c_1		

$$\mathcal{F} = \{ \textcircled{A B \rightarrow C}, \underline{C \rightarrow A} \}$$

BCNF? ✓ a superkey?
✓ a superkey!

$$R_2 : \{ CA \} \quad \mathcal{F}_2 : \{ C \rightarrow A \}$$

$$R_1 : \{ BC \} \quad \mathcal{F}_1 : \{ \cancel{C \rightarrow B} \} ?$$



$$\mathcal{T} = \{ A \rightarrow B, (B \rightarrow C), \cancel{A \rightarrow C} \}$$

$$\mathcal{T} = \left\{ \frac{A \cancel{B} \rightarrow C}{A \rightarrow B} \right\} \quad \times \quad \begin{matrix} A \rightarrow C \\ B \rightarrow C \end{matrix}$$

$$\mathcal{T} \models \underline{A} \rightarrow \underline{B} C$$

false $AB \rightarrow C \models A \rightarrow C$

True $\underline{A \rightarrow C} \models \underline{AB \rightarrow C}$

$$\mathcal{T} = \{A \rightarrow C\}$$

$$\mathcal{T} \models AB \rightarrow C$$

$$\begin{aligned} AB \rightarrow BC \\ \equiv \frac{A \cancel{B} \rightarrow B}{AB \rightarrow C} \end{aligned}$$